Einführung in die Computerlinguistik HMMs

Hinrich Schütze

Center for Information and Language Processing

2018-12-17





3 POS tagging

POS setup

5 Probabilistic POS tagging





2 Basics

3 POS tagging

POS setup

5 Probabilistic POS tagging



Definition

Statistical Natural Language Processing (StatNLP) uses methods of supervised, semisupervised and unsupervised learning to address tasks that involve written or spoken (human) language.

Adjective for "statistics"

 $\mathsf{statistics} = \mathsf{the}\ \mathsf{practice}\ \mathsf{or}\ \mathsf{science}\ \mathsf{of}\ \mathsf{collecting}\ \mathsf{and}\ \mathsf{analyzing}\ \mathsf{numerical}\ \mathsf{data}$

statistics vs. machine learning

Adjective for "statistics"

 $\mathsf{statistics} = \mathsf{the}\ \mathsf{practice}\ \mathsf{or}\ \mathsf{science}\ \mathsf{of}\ \mathsf{collecting}\ \mathsf{and}\ \mathsf{analyzing}\ \mathsf{numerical}\ \mathsf{data}$

Statistical parameter estimation

an important / the most important subfield of machine learning

statistics vs. machine learning

automatic summarization of text

- automatic summarization of text
- sentiment analysis (e.g., find all *negative* reviews of the smartphone I want to buy)

- automatic summarization of text
- sentiment analysis (e.g., find all *negative* reviews of the smartphone I want to buy)
- information extraction from text (e.g., find all inhibitors of a particular gene)

- automatic summarization of text
- sentiment analysis (e.g., find all *negative* reviews of the smartphone I want to buy)
- information extraction from text (e.g., find all inhibitors of a particular gene)
- machine translation

- automatic summarization of text
- sentiment analysis (e.g., find all *negative* reviews of the smartphone I want to buy)
- information extraction from text (e.g., find all inhibitors of a particular gene)
- machine translation

Applications that use some StatNLP

speech recognition optical character recognition information retrieval

• 1940s, early 1950s: language as sequential process, Markov models

- 1940s, early 1950s: language as sequential process, Markov models
- 1950s, 1960s: Chomsky; statistical methods are viewed as inadequate for language.

- 1940s, early 1950s: language as sequential process, Markov models
- 1950s, 1960s: Chomsky; statistical methods are viewed as inadequate for language.
- 1970s, 1980s: very little academic research on StatNLP, but IBM Watson group does seminal work

- 1940s, early 1950s: language as sequential process, Markov models
- 1950s, 1960s: Chomsky; statistical methods are viewed as inadequate for language.
- 1970s, 1980s: very little academic research on StatNLP, but IBM Watson group does seminal work
- 1990s: IBM Watson paradigm is adopted by computational linguists and becomes dominant approach to natural language processing.

- 1940s, early 1950s: language as sequential process, Markov models
- 1950s, 1960s: Chomsky; statistical methods are viewed as inadequate for language.
- 1970s, 1980s: very little academic research on StatNLP, but IBM Watson group does seminal work
- 1990s: IBM Watson paradigm is adopted by computational linguists and becomes dominant approach to natural language processing.
- 2000s: The field splits methodologically into three communities.

- 1940s, early 1950s: language as sequential process, Markov models
- 1950s, 1960s: Chomsky; statistical methods are viewed as inadequate for language.
- 1970s, 1980s: very little academic research on StatNLP, but IBM Watson group does seminal work
- 1990s: IBM Watson paradigm is adopted by computational linguists and becomes dominant approach to natural language processing.
- 2000s: The field splits methodologically into three communities.
 - traditional computational linguistics

- 1940s, early 1950s: language as sequential process, Markov models
- 1950s, 1960s: Chomsky; statistical methods are viewed as inadequate for language.
- 1970s, 1980s: very little academic research on StatNLP, but IBM Watson group does seminal work
- 1990s: IBM Watson paradigm is adopted by computational linguists and becomes dominant approach to natural language processing.
- 2000s: The field splits methodologically into three communities.
 - traditional computational linguistics
 - a large group of researchers that use existing statistical methods

- 1940s, early 1950s: language as sequential process, Markov models
- 1950s, 1960s: Chomsky; statistical methods are viewed as inadequate for language.
- 1970s, 1980s: very little academic research on StatNLP, but IBM Watson group does seminal work
- 1990s: IBM Watson paradigm is adopted by computational linguists and becomes dominant approach to natural language processing.
- 2000s: The field splits methodologically into three communities.
 - traditional computational linguistics
 - a large group of researchers that use existing statistical methods
 - a small group of researchers that do active research on machine learning methods

Recent big success story 1



StatNLP Basics POS tagging POS setup Probabilistic POS tagging Viterbi Schütze: HMMs

Recent big success story 2

Siri. 2017 Your wish is its command.

Siri on iPhone 45 lets you use your voice to send messages, schedule meetings, place phone calls, and more. Ask Siri to do things just by talking the way you talk. Siri understands what you say, knows what you mean, and even talks back. Siri is so easy to use and does so much, you'll keep finding more and more ways to use it.



Google Translate - more on this later





- POS setup
- **5** Probabilistic POS tagging



max

 $\max_{x} f(x)$ the largest value of f(x)

argmax

 $\operatorname{argmax}_{x} f(x)$ that value of x for which f(x) is largest

•
$$\max_x(-(x-2)^2+5)$$

•
$$\operatorname{argmax}_{x}(-(x-2)^{2}+5)$$

$$\operatorname{argmax}_{x} f(x) = \operatorname{argmax}_{x} c \cdot f(x)$$

$$\operatorname{argmax}_{x} f(x) = \operatorname{argmax}_{x} 1/c \cdot f(x)$$

$$\sum$$

$$\sum_{i=m}^{i=n} f(i) = f(m) + f(m+1) + \ldots + f(n-1) + f(n)$$

Π

$$\prod_{i=m}^{i=n} f(i) = f(m) \cdot f(m+1) \cdot \ldots \cdot f(n-1) \cdot f(n)$$

$$\sum_{i=5}^{i=8} i^2 = \prod_{i=0}^{i=3} (i+1) =$$

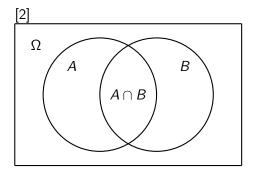
• The joint probability P(AB) is the probability that A and B occur together / at the same time (i.e., jointly).

- The joint probability P(AB) is the probability that A and B occur together / at the same time (i.e., jointly).
- We can write *P*(*AB*) as *P*(*A*∩*B*) if *A* and *B* are formalized as sets.

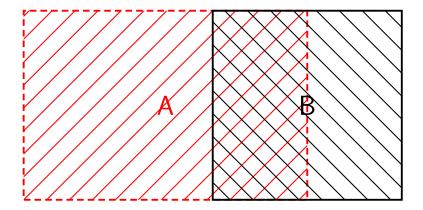
• The conditional probability is the updated probability of an event given some knowledge.

- The conditional probability is the updated probability of an event given some knowledge.
- Definition: $P(A|B) = \frac{P(AB)}{P(B)} (P(B) > 0)$

Venn diagram



To compute P(A|B): Divide the area of $A \cap B$ by the area of B. $P(A|B) = P(A \cap B)/P(B)$ $P(B|A) = P(A \cap B)/P(A)$



Compute $P(A|B) = P(A \cap B)/P(B)$ and $P(B|A) = P(A \cap B)/P(A)$

$$P(X_1X_2X_3\ldots X_n) =$$

$$P(X_1) \cdot P(X_2|X_1) \cdot P(X_3|X_1X_2) \cdot \ldots \cdot P(X_n|X_1X_2 \ldots X_{n-1})$$

•
$$P(B|A) = \frac{P(BA)}{P(A)} = \frac{P(A|B)P(B)}{P(A)}$$

•
$$P(B|A) = \frac{P(BA)}{P(A)} = \frac{P(A|B)P(B)}{P(A)}$$

• Or: $P(B|A) = \frac{P(A|B)P(B)}{P(A|B)P(B)+P(A|\overline{B})P(\overline{B})}$

•
$$P(B|A) = \frac{P(BA)}{P(A)} = \frac{P(A|B)P(B)}{P(A)}$$

• Or: $P(B|A) = \frac{P(A|B)P(B)}{P(A|B)P(B)+P(A|\overline{B})P(\overline{B})}$
• Follows from

$$P(A) = P(AB) + P(A\overline{B}) = P(A|B)P(B) + P(A|\overline{B})P(\overline{B})$$

• Two events A and B are independent iff P(AB) = P(A)P(B)

- Two events A and B are independent iff P(AB) = P(A)P(B)
- If I learn that A is true, then that doesn't change my assessment of the probability of B (and vice versa).

- Two events A and B are independent iff P(AB) = P(A)P(B)
- If I learn that A is true, then that doesn't change my assessment of the probability of B (and vice versa).
- If A and B are independent, then: P(A) = P(A|B), P(B) = P(B|A)

• Estimate P(A), P(B), P(AB)

• Estimate P(A), P(B), P(AB)

• Simplest way of doing this: relative frequency: $P(A) = \frac{\text{count}(A)}{\text{count}(everything)}$

• Estimate P(A), P(B), P(AB)

- Simplest way of doing this: relative frequency: $P(A) = \frac{\text{count}(A)}{\text{count}(everything)}$
- Then: Compare P(A)P(B) with P(AB)

• Estimate P(A), P(B), P(AB)

- Simplest way of doing this: relative frequency: $P(A) = \frac{\text{count}(A)}{\text{count}(everything)}$
- Then: Compare P(A)P(B) with P(AB)
- Recall: A, B independent iff P(AB) = P(A)P(B)

- Estimate P(A), P(B), P(AB)
- Simplest way of doing this: relative frequency: $P(A) = \frac{\text{count}(A)}{\text{count}(everything)}$
- Then: Compare P(A)P(B) with P(AB)
- Recall: A, B independent iff P(AB) = P(A)P(B)
- P(AB) ≫ P(A)P(B): This indicates A and B are strongly dependent (and positively correlated).

- Estimate P(A), P(B), P(AB)
- Simplest way of doing this: relative frequency: $P(A) = \frac{\text{count}(A)}{\text{count}(everything)}$
- Then: Compare P(A)P(B) with P(AB)
- Recall: A, B independent iff P(AB) = P(A)P(B)
- P(AB) >> P(A)P(B): This indicates A and B are strongly dependent (and positively correlated).
- P(AB) ≈ P(A)P(B): This indicates A and B are independent.

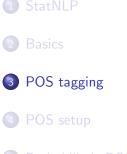
- Estimate P(A), P(B), P(AB)
- Simplest way of doing this: relative frequency: $P(A) = \frac{\text{count}(A)}{\text{count}(everything)}$
- Then: Compare P(A)P(B) with P(AB)
- Recall: A, B independent iff P(AB) = P(A)P(B)
- P(AB) ≫ P(A)P(B): This indicates A and B are strongly dependent (and positively correlated).
- P(AB) ≈ P(A)P(B): This indicates A and B are independent.
- P(AB) ≪ P(A)P(B): This indicates A and B are strongly dependent (and negatively correlated).

- Estimate P(A), P(B), P(AB)
- Simplest way of doing this: relative frequency: $P(A) = \frac{\text{count}(A)}{\text{count}(everything)}$
- Then: Compare P(A)P(B) with P(AB)
- Recall: A, B independent iff P(AB) = P(A)P(B)
- P(AB) >> P(A)P(B): This indicates A and B are strongly dependent (and positively correlated).
- P(AB) ≈ P(A)P(B): This indicates A and B are independent.
- P(AB) ≪ P(A)P(B): This indicates A and B are strongly dependent (and negatively correlated).
- Why \approx ?

A = champagne, B = sparkling

Übung

Find either two independent words or two words that occur less often on the same page than expected by chance







• Part-of-speech tagging is the process of disambiguating the syntactic category of a word in context.

- Part-of-speech tagging is the process of disambiguating the syntactic category of a word in context.
- Example: "book" is either a verb or a noun.

- Part-of-speech tagging is the process of disambiguating the syntactic category of a word in context.
- Example: "book" is either a verb or a noun.
- In the context "the book" it can only be a noun.

- Part-of-speech tagging is the process of disambiguating the syntactic category of a word in context.
- Example: "book" is either a verb or a noun.
- In the context "the book" it can only be a noun.
- In the context "to book a flight" it can only be a verb.

- Part-of-speech tagging is the process of disambiguating the syntactic category of a word in context.
- Example: "book" is either a verb or a noun.
- In the context "the book" it can only be a noun.
- In the context "to book a flight" it can only be a verb.
- Part-of-speech tagging assigns to "book" the correct syntactic category in context.

• The example of "book" in the phrase "the book" is easy.

- The example of "book" in the phrase "the book" is easy.
- The rule "a word after 'the' cannot be a verb" takes care of it.

- The example of "book" in the phrase "the book" is easy.
- The rule "a word after 'the' cannot be a verb" takes care of it.
- Are all cases of part-of-speech tagging this easy?

The representative put chairs on the table

The	representative	put	chairs	on	the	table
AT	NN	VBD	NNS	IN	AT	NN
article	noun	verb-d	noun-s	prep	article	noun

The	representative	put	chairs	on	the	table
AT	NN	VBD	NNS	IN	AT	NN
article	noun	verb-d	noun-s	prep	article	noun

The	representative	put	chairs	on	the	table
AT	NN	VBD	NNS		AT	NN
article	noun	verb-d	noun-s		article	noun
AT	JJ	NN	VBZ	IN	AT	NN
article	adjective	noun	verb-z	prep	article	noun

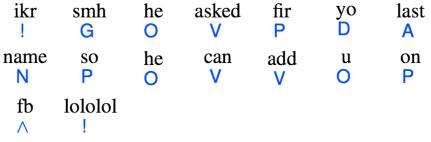
The	representative	put	chairs	on	the	table
AT	NN	VBD	NNS		AT	NN
article	noun	verb-d	noun-s		article	noun
AT	JJ	NN	VBZ	IN	AT	NN
article	adjective	noun	verb-z	prep	article	noun

In this case, finding the correct parts of speech for the sentence is more difficult.

• Part-of-speech tagging is used as a preprocessing step.

- Part-of-speech tagging is used as a preprocessing step.
- It is solvable: Very high accuracy rates can be achieved (95–98%).

- Part-of-speech tagging is used as a preprocessing step.
- It is solvable: Very high accuracy rates can be achieved (95–98%).
- It helps with many things you want to do with text, e.g., chunking, information extraction, question answering and parsing.



Tagging is a preprocessing step for man NLP tasks.



2 Basics

3 POS tagging



5 Probabilistic POS tagging



• We will first look at the Brown corpus tag set.

- We will first look at the Brown corpus tag set.
- Early work on part-of-speech tagging was done on the Brown corpus.

- We will first look at the Brown corpus tag set.
- Early work on part-of-speech tagging was done on the Brown corpus.
- It's still an important corpus in NLP.

Creators of Brown corpus: W. Nelson Francis & Henry Kučera (Brown University)



Brown part-of-speech tags

Tag	Part Of Speech					
AT	article	Tag	Part Of Speech			
BEZ	the word "is"	RB	adverb			
IN	preposition	RBR	comparative adverb			
JJ	adjective	ТО	the word "to"			
JJR	comparative adjective	VB	verb, base form			
MD	modal	VBD	verb, past tense			
NN	singular or mass noun	VBG	verb, present participle, gerund			
NNP	singular proper noun	VBN	verb, past participle			
NNS	plural noun	VBZ	verb, 3rd singular present			
PERIOD	. : ? !	WDT	wh-determiner: "what", "which",			
PN	personal pronoun					
Are these typical syntactic estagories?						

Are these typical syntactic categories?

Tag: "Peter arrived in London on Tuesday"

- Let's look again at our example sentence: "The representative put chairs on the table."
- What information is available to disambiguate this sentence syntactically?

[2] The following sentence is ambiguous wrt POS. Why?

The	representative	put	chairs	on	the	table
AT	NN	VBD	NNS		AT	NN
article	noun	verb-d	noun-s		article	noun
AT	JJ	NN	VBZ		AT	NN
article	adjective	noun	verb-z		article	noun

The context of the ambiguous word: the words to the left and to the right

The context of the ambiguous word: the words to the left and to the right

• Example: for a JJ/NN ambiguity in the context "AT _ VBZ", NN is much more likely than JJ.

- The context of the ambiguous word: the words to the left and to the right
 - Example: for a JJ/NN ambiguity in the context "AT _ VBZ", NN is much more likely than JJ.
- A word's bias for the different parts of speech

- The context of the ambiguous word: the words to the left and to the right
 - Example: for a JJ/NN ambiguity in the context "AT _ VBZ", NN is much more likely than JJ.
- A word's bias for the different parts of speech
 - Example: "put" is much more likely to occur as a VBD than as an NN.

• Information source 2: The frequency of the different parts of speech of the ambiguous word

- Information source 2: The frequency of the different parts of speech of the ambiguous word
- This source of information lets us do 90% correct tagging of English very easily: Just pick the most frequent tag for each word.

- Information source 2: The frequency of the different parts of speech of the ambiguous word
- This source of information lets us do 90% correct tagging of English very easily: Just pick the most frequent tag for each word.
- For most words in English, the distribution of tags is very uneven: there is one very frequent tag and the others are rare.

[2] the word at position i in the corpus W; ti the tag of w; w^{\prime} the *I*th word in the lexicon ť the i^{th} tag in the tag set C(w')the number of occurrences of w^{l} in the training set $C(t^j)$ the number of occurrences of t^{j} in the training set $C(t^j t^k)$ the number of occurrences of t^j followed by t^k $C(w':t^j)$ the number of occurrences of w^{l} that are tagged as t^{j}

Notation: Example

the	representative	put	chairs	on	the	table
w ₁	<i>W</i> ₂	W3	W4	W5	w ₆	W ₇
w ⁵	w ⁸¹	w ³	w ⁴	w ¹	w ⁵	w ⁶
AT	NN	VBD	NNS	IN	AT	NN
article	noun	verb-d	noun-s	prep	article	noun
t_1	t_2	t ₃	t4	t5	t_6	t7
t ¹⁶	t^{12}	t ²	t ⁹	t ³	t ¹⁶	t ¹²

$$\begin{array}{ccccc} C(w^5) & = & 2 & | & C(w^4) & = & 1 \\ C(t^{16}) & = & 2 & | & C(t^2) & = & 1 \\ C(t^{16}t^{12}) & = & 2 & | & C(t^{12}t^2) & = & 1 \\ C(t^{16}t^2) & = & 0 & | & C(w^5w^{81}) & = & 1 \\ C(w^5:t^{16}) & = & 2 & | & C(w^5:t^{12}) & = & 0 \end{array}$$

Notation: Übung

Confidence/NN in/IN the/AT pound/NN is/BEZ widely/RB expected/VBN to/TO take/VB another/AT sharp/JJ dive/NN if/IN trade/NN figures/NNS for/IN September/NNP ,/, due/JJ for/IN release/NN tomorrow/NN ,/, fail/VB to/TO show/VB a/AT substantial/JJ improvement/NN from/IN July/NNP and/CC August/NNP 's/POS near-record/JJ deficits/NNS ./. Chancellor/NNP of/IN the/AT Exchequer/NNP Nigel/NNP Lawson/NNP 's/POS restated/VBN commitment/NN to/TO a/AT firm/JJ monetary/JJ policy/NN has/VBZ helped/VBN to/TO prevent/VB a/AT freefall/NN in/IN sterling/NN over/IN the/AT past/JJ week/NN ./.

Give the values of the following: w_4 , t_5 , $C(w_8)$, $C(t_9)$, $C(t_1t_2)$, $C(w_3:t_3)$

• Labeled training set: each word is annotated (or marked or tagged) by a linguist, with correct part-of-speech

- Labeled training set: each word is annotated (or marked or tagged) by a linguist, with correct part-of-speech
- Train a statistical model on the training set

- Labeled training set: each word is annotated (or marked or tagged) by a linguist, with correct part-of-speech
- Train a statistical model on the training set
 - Result: A set of parameters (= numbers) that were learned from the specific properties of the training set

- Labeled training set: each word is annotated (or marked or tagged) by a linguist, with correct part-of-speech
- Train a statistical model on the training set
 - Result: A set of parameters (= numbers) that were learned from the specific properties of the training set
- Apply statistical model to new text that we want to analyze for some task (information retrieval, machine translation etc)

Confidence/NN in/IN the/AT pound/NN is/BEZ widely/RB expected/VBN to/TO take/VB another/AT sharp/JJ dive/NN if/IN trade/NN figures/NNS for/IN September/NNP ,/, due/JJ for/IN release/NN tomorrow/NN ,/, fail/VB to/TO show/VB a/AT substantial/JJ improvement/NN from/IN July/NNP and/CC August/NNP 's/POS near-record/JJ deficits/NNS ./. Chancellor/NNP of/IN the/AT Exchequer/NNP Nigel/NNP Lawson/NNP 's/POS restated/VBN commitment/NN to/TO a/AT firm/JJ monetary/JJ policy/NN has/VBZ helped/VBN to/TO prevent/VB a/AT freefall/NN in/IN sterling/NN over/IN the/AT past/JJ week/NN ./.



2 Basics

3 POS tagging

POS setup

5 Probabilistic POS tagging

6 Viterbi

- Parameter estimation: context parameters
- Parameter estimation: bias parameters
- Greedy tagging
- Viterbi tagging

- The conditional probabilities $P(t^k|t^j)$ are the context parameters of the model.
- This will be our formalization of the first source of information in tagging: the context.
- Note that this is a very impoverished model of context.
 - Limited horizon, Markov assumption: we assume that our memory is limited to a single preceding tag.
 - Time invariance, stationary: we assume that these conditional probabilities don't change. (e.g., the same at the beginning and at the end of the sentence)

• How can we estimate $P(t^k|t^j)$?

- How can we estimate $P(t^k|t^j)$?
- For example: how can we estimate P(NN|JJ)?

- How can we estimate $P(t^k|t^j)$?
- For example: how can we estimate P(NN|JJ)?
- First: maximum likelihood estimate

- How can we estimate $P(t^k|t^j)$?
- For example: how can we estimate P(NN|JJ)?
- First: maximum likelihood estimate
- Training text: long tagged sequence of words

Confidence/NN in/IN the/AT pound/NN is/BEZ widely/RB expected/VBN to/TO take/VB another/AT sharp/JJ dive/NN if/IN trade/NN figures/NNS for/IN September/NNP ,/, due/JJ for/IN release/NN tomorrow/NN ,/, fail/VB to/TO show/VB a/AT substantial/JJ improvement/NN from/IN July/NNP and/CC August/NNP 's/POS near-record/JJ deficits/NNS ./. Chancellor/NNP of/IN the/AT Exchequer/NNP Nigel/NNP Lawson/NNP 's/POS restated/VBN commitment/NN to/TO a/AT firm/JJ monetary/JJ policy/NN has/VBZ helped/VBN to/TO prevent/VB a/AT freefall/NN in/IN sterling/NN over/IN the/AT past/JJ week/NN ./.

Parameter estimation: Context

۲

٢

• How can we estimate $P(t^k|t^j)$?

- For example: how can we estimate P(NN|JJ)?
- ml = maximum likelihood = relative frequency

 $\hat{P}_{ml}(t^k|t^j) = \frac{\hat{P}_{ml}(t^jt^k)}{\hat{P}_{ml}(t^j)} \approx \frac{\frac{C(t^jt^k)}{C(.)}}{\frac{C(t^j)}{C(.)}} = \frac{C(t^jt^k)}{C(t^j)}$

$$\hat{P}_{ml}(NN|JJ) = \frac{C(JJ NN)}{C(JJ)}$$

In an *n*th order Markov model,

the tag at time t depends on the n previous tags.

- Order 0: Tag does not depend on previous tags.
- Order 1: Tag depends on immediately preceding tag.
- Order 2: Tag depends on two immediately preceding tags.
- Order 3: Tag depends on three immediately preceding tags....

(analogous for Markov model that emits words instead of tags)

- What about the second source of information: frequency of different tags for a word?
- We need to estimate: $P(t_i|w_i)$
- Actually: $P(w_i|t_i)$
- Example: P(book|NN)

- What about the second source of information: frequency of different tags for a word?
- We need to estimate: $P(t_i|w_i)$
- Actually: $P(w_i|t_i)$
- Example: P(book|NN)

- What about the second source of information: frequency of different tags for a word?
- We need to estimate: $P(t_i|w_i)$
- Actually: $P(w_i|t_i)$
- Example: P(book|NN)

- What about the second source of information: frequency of different tags for a word?
- We need to estimate: $P(t_i|w_i)$
- Actually: $P(w_i|t_i)$
- Example: P(book|NN)

- What about the second source of information: frequency of different tags for a word?
- We need to estimate: $P(t_i|w_i)$
- Actually: $P(w_i|t_i)$
- Example: P(book|NN)

Parameter estimation: Word bias

• How to estimate P(book|NN)

۲

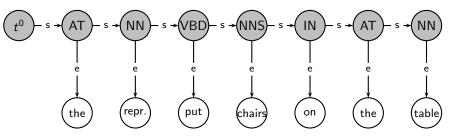
$$\hat{P}_{ml}(w^{l}|t^{j}) = \frac{\hat{P}_{ml}(w^{l}:t^{j})}{\hat{P}_{ml}(t^{j})} = \frac{\frac{C(w^{l}:t^{j})}{C(.)}}{\frac{C(t^{j})}{C(.)}} = \frac{C(w^{l}:t^{j})}{C(t^{j})}$$
$$\hat{P}_{ml}(\text{book}|\text{NN}) = \frac{C(\text{book}:\text{NN})}{C(\text{NN})}$$

Confidence/NN in/IN the/AT pound/NN is/BEZ widely/RB expected/VBN to/TO take/VB another/AT sharp/JJ dive/NN if/IN trade/NN figures/NNS for/IN September/NNP ,/, due/JJ for/IN release/NN tomorrow/NN ,/, fail/VB to/TO show/VB a/AT substantial/JJ improvement/NN from/IN July/NNP and/CC August/NNP 's/POS near-record/JJ deficits/NNS ./. Chancellor/NNP of/IN the/AT Exchequer/NNP Nigel/NNP Lawson/NNP 's/POS restated/VBN commitment/NN to/TO a/AT firm/JJ monetary/JJ policy/NN has/VBZ helped/VBN to/TO prevent/VB a/AT freefall/NN in/IN sterling/NN over/IN the/AT past/JJ week/NN ./.

Estimate P(take|VB) and P(AT|IN)

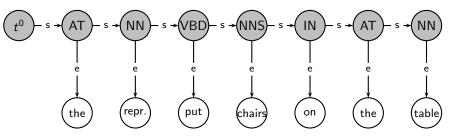
- What about the second source of information: frequency of different tags for a word?
- We need to estimate: $P(t_i|w_i)$
- Actually: $P(w_i|t_i)$
- Example: P(book|NN)

(s = sequence, e = emission)



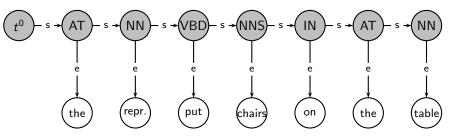
- The tags generate the words (not vice versa).
- Hence: The tags are given and the words are conditioned on the tags ...
- ... and the correct formalization is P(w|t).

(s = sequence, e = emission)



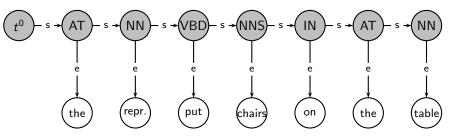
- The tags generate the words (not vice versa).
- Hence: The tags are given and the words are conditioned on the tags ...
- ... and the correct formalization is P(w|t).

(s = sequence, e = emission)



- The tags generate the words (not vice versa).
- Hence: The tags are given and the words are conditioned on the tags ...
- ... and the correct formalization is P(w|t).

(s = sequence, e = emission)



- The tags generate the words (not vice versa).
- Hence: The tags are given and the words are conditioned on the tags ...
- ... and the correct formalization is P(w|t).

- Context: $P(t_{i+1}|t_i)$
- Word bias: $P(w_i|t_i)$
- Given a sequence of words (a sentence), how do we compute the corresponding (disambiguated) part-of-speech sequence?
- Example:
 - Input: the representative put chairs on the table
 - Output: AT NN VBD NNS IN AT NN
- How can we do this?

- Suppose we've tagged a sentence up to position *i*.
- Then simply choose the tag t for the next word w_{i+1} that is most probable.
- At position *i*, choose tag that maximizes:
 P(t_i|t_{i-1})P(w_i|t_i)
- Let's do this for: "The representative put chairs on the table."
- P(VBD|NN)P(put|VBD)
- $t_3 = \text{VBD}$ maximizes $P(t_3|\text{NN})P(\text{put}|t_3)$

- What can go wrong with greedy tagging?
- Example?
- A representative put costs 20% more today than a month ago.

Notation (2)

[2]	
Wi	the word at position <i>i</i> in the corpus
ti	the tag of w _i
Wi,i+m	the words occurring at positions i through $i + m$
	(alternative notations: $w_i \cdots w_{i+m}, w_i, \dots, w_{i+m}, w_{i(i+m)}$)
$t_{i,i+m}$	the tags $t_i \cdots t_{i+m}$ for $w_i \cdots w_{i+m}$
w ¹	the I th word in the lexicon
t ^j	the j th tag in the tag set
C(w')	the number of occurrences of w' in the training set
$C(t^j)$	the number of occurrences of t^j in the training set
$C(t^j t^k)$	the number of occurrences of t^j followed by t^k
$C(w':t^j)$	the number of occurrences of w^{I} that are tagged as t^{j}
Т	number of tags in tag set
W	number of words in the lexicon
п	sentence length

[2]

• We define our goal thus: Given a sentence, find the most probable sequence of tags for this sentence.

[2]

- We define our goal thus: Given a sentence, find the most probable sequence of tags for this sentence.
- Formalization of this goal:

$$t_{1,n} = \operatorname{argmax}_{t_{1,n}} P(t_{1,n}|w_{1,n})$$

$$t_{1,n} = \operatorname{argmax}_{t_{1,n}} P(t_{1,n}|w_{1,n})$$
 (1)

$$= \operatorname{argmax}_{t_{1,n}} P(t_{0,n} | w_{1,n})$$
(2)

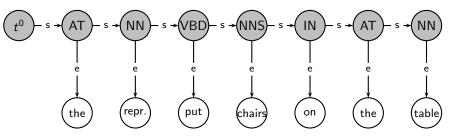
$$= \operatorname{argmax}_{t_{1,n}} \frac{P(w_{1,n}|t_{0,n})P(t_{0,n})}{P(w_{1,n})}$$
(3)

$$= \operatorname{argmax}_{t_{1,n}} P(w_{1,n}|t_{0,n}) P(t_{0,n})$$
(4)

$$= \operatorname{argmax}_{t_{1,n}} [\prod_{i=1}^{n} P(w_i | t_{0,n})] P(t_{0,n})$$
(5)

2: dummy "start" tag; 3: Bayes; 4: positive factor doesn't affect argmax; 5: assumption: words are independent

(s = sequence, e = emission)



- The tags generate the words (not vice versa).
- Hence: The tags are given and the words are conditioned on the tags ...
- ... and the correct formalization is P(w|t).

Simplifying the argmax (2)

$$= \operatorname{argmax}_{t_{1,n}} [\prod_{i=1}^{n} P(w_i|t_i)] P(t_{0,n})$$
(6)
$$= \operatorname{argmax}_{t_{1,n}} [\prod_{i=1}^{n} P(w_i|t_i)] [\prod_{i=1}^{n} P(t_i|t_{0,i-1})]$$
(7)
$$= \operatorname{argmax}_{t_{1,n}} [\prod_{i=1}^{n} P(w_i|t_i)] [\prod_{i=1}^{n} P(t_i|t_{i-1})]$$
(8)
$$= \operatorname{argmax}_{t_{1,n}} \prod_{i=1}^{n} [P(w_i|t_i) P(t_i|t_{i-1})]$$
(9)

7: chain rule; 8: Markov assumption; 9:
$$\prod_{i=1}^{n} x_i \prod_{i=1}^{n} y_i = \prod_{i=1}^{n} x_i y_i$$

$$= \operatorname{argmax}_{t_{1,n}} \prod_{i=1}^{n} [P(w_i|t_i)P(t_i|t_{i-1})]$$
(10)
$$= \operatorname{argmax}_{t_{1,n}} \sum_{i=1}^{n} [\log P(w_i|t_i) + \log P(t_i|t_{i-1})]$$
(11)

11: computation in log space more efficient / convenient

Do you recognize these parameters?

1 StatNLP

2 Basics

3 POS tagging

POS setup

5 Probabilistic POS tagging



$$\operatorname{argmax}_{t_{1,n}} \sum_{i=1}^{n} [\log P(w_i|t_i) + \log P(t_i|t_{i-1})]$$

What's the difficulty if you want to tag based on this?

$$\operatorname{argmax}_{t_{1,n}} \sum_{i=1}^{n} [\log P(w_i|t_i) + \log P(t_i|t_{i-1})]$$

There are $|T|^n$ different tag sequences. E.g.: $40^{20} = 109,951,162,777,600,000,000,000,000,000$ Is there a better way?

Dynamic programming: Viterbi

- Optimal substructure: The optimal solution to the problem contains within it subsolutions, i.e., optimal solutions to subproblems.
- Overlapping subsolutions: The subsolutions overlap. These subsolutions are computed over and over again when computing the global optimal solution in a brute-force algorithm.
- Subproblem in the case of tagging: what is the best path (tag sequence) that gets me to tag t at position j?
- Overlapping subsolutions: The best path that gets me to tag t at position j is needed for computing all T paths at position $j+1 \ldots$
- ... but I only compute it once!

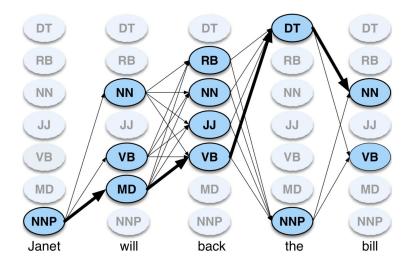
$\frac{P(t_i|t_{i-1})}{\text{Example: } P(\text{VB}|\text{MD}) = 0.7968}$

	NNP	MD	VB	JJ	NN	RB	DT
< s >	0.2767	0.0006	0.0031	0.0453	0.0449	0.0510	0.2026
NNP	0.3777	0.0110	0.0009	0.0084	0.0584	0.0090	0.0025
MD	0.0008	0.0002	0.7968	0.0005	0.0008	0.1698	0.0041
VB	0.0322	0.0005	0.0050	0.0837	0.0615	0.0514	0.2231
JJ	0.0366	0.0004	0.0001	0.0733	0.4509	0.0036	0.0036
NN	0.0096	0.0176	0.0014	0.0086	0.1216	0.0177	0.0068
RB	0.0068	0.0102	0.1011	0.1012	0.0120	0.0728	0.0479
DT	0.1147	0.0021	0.0002	0.2157	0.4744	0.0102	0.0017

P(w|t)Example: P(the|DT) = 0.506099

	Janet	will	back	the	bill
NNP	0.000032	0	0	0.000048	0
MD	0	0.308431	0	0	0
VB	0	0.000028	0.000672	0	0.000028
JJ	0	0	0.000340	0	0
NN	0	0.000200	0.000223	0	0.002337
RB	0	0	0.010446	0	0
DT	0	0	0	0.506099	0

Key idea of Viterbi: Lattice



Schütze: HMMs

Viterbi

function VITERBI(observations of len T, state-graph of len N) returns best-path, path-prob

create a path probability matrix viterbi[N,T] for each state s from 1 to N do : initialization step *viterbi*[*s*,1] $\leftarrow \pi_s * b_s(o_1)$ *backpointer*[s,1] $\leftarrow 0$ for each time step t from 2 to T do : recursion step for each state s from 1 to N do $viterbi[s,t] \leftarrow \max_{s'=1}^{N} viterbi[s',t-1] * a_{s',s} * b_s(o_t)$ backpointer[s,t] \leftarrow argmax viterbi[s',t-1] * a_{s',s} * b_s(o_t) s'=1 $bestpathprob \leftarrow \max_{s=1}^{N} viterbi[s,T]$; termination step $bestpathpointer \leftarrow argmax viterbi[s,T]$; termination step *bestpath*

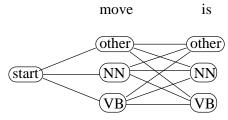
— the path starting at state *bestpathpointer*, that follows backpointer[] to states back in time return bestpath, bestpathprob

$P(t_i|t_{i-1})$ Example: P(VB|NN) = 0.5

next	other	ΝN	VB
	0.3	0.4	0.3
	0.2	0.2	0.6
	0.4	0.1	0.5
	0.1	0.8	0.1
	next	0.3 0.2 0.4	0.2 0.2 0.4 0.1

P(w|t)Example: P(bear|NN) = 0.45

	other	NN	VB
bear	0.1	0.45	0.4
is	0.3	0.05	0.05
on	0.3	0.05	0.05
the	0.2	0.05	0.05
move	0.1	0.4	0.45



Goal: Compute

$$\arg\max_{t_1,t_2}p(t_1,\textit{move},t_2,\textit{is}) =$$

$$\arg\max_{t_1,t_2} p(t_1|start)p(move|t_1)p(t_2|t_1)p(is|t_2)$$

viterbi = vtrb backpointer = bptr lattice = path probability matrix vtrb_j(t_i) is the probability of [the most probable path from 0 to j that tags word w_j with tag t_i].

 $bptr_j(t_i)$ is the tag of w_{j-1} on [the most probable path from 0 to j that tags word w_j with tag t_i].

Initialization: $vtrb_0(start) = 1$

 $\begin{array}{l} vtrb_1(other) = vtrb_0(start) \ p(other|start) \ p(move|other) = 1.0 * 0.3 * 0.1 = 0.03 \\ vtrb_1(NN) = vtrb_0(start) \ p(NN|start) \ p(move|NN) = 1.0 * 0.4 * 0.4 = 0.16 \\ vtrb_1(VB) = vtrb_0(start) \ p(VB|start) \ p(move|VB) = 1.0 * 0.3 * 0.45 = 0.135 \end{array}$

$$\begin{array}{l} vtrb_2(other) = max(\\ vtrb_1(other) \ p(other|other) \ p(is|other) = 0.03 * 0.2 * 0.3 = 0.0018, \\ vtrb_1(NN) \ p(other|NN) \ p(is|other) = 0.16 * 0.4 * 0.3 = 0.0192, \\ vtrb_1(VB) \ p(other|VB) \ p(is|other) = 0.135 * 0.1 * 0.3 = 0.00405 \\) = 0.0192 \\ bptr_2(other) = NN \end{array}$$

$$\begin{array}{l} \mathsf{vtrb}_2(\mathsf{NN}) = \mathsf{max}(\\ \mathsf{vtrb}_1(\mathsf{other}) \; \mathsf{p}(\mathsf{NN}|\mathsf{other}) \; \mathsf{p}(\mathsf{is}|\mathsf{NN}) = 0.03 * 0.2 * 0.05 = 0.0003, \\ \mathsf{vtrb}_1(\mathsf{NN}) \; \mathsf{p}(\mathsf{NN}|\mathsf{NN}) \; \mathsf{p}(\mathsf{is}|\mathsf{NN}) = 0.16 * 0.1 * 0.05 = 0.0008, \\ \mathsf{vtrb}_1(\mathsf{VB}) \; \mathsf{p}(\mathsf{NN}|\mathsf{VB}) \; \mathsf{p}(\mathsf{is}|\mathsf{NN}) = 0.135 * 0.8 * 0.05 = 0.0054 \\) = 0.0054 \\ \mathsf{bptr}_2(\mathsf{NN}) = \mathsf{VB} \end{array}$$

$$\begin{array}{l} \mathsf{vtrb}_2(\mathsf{VB}) = \mathsf{max}(\\ \mathsf{vtrb}_1(\mathsf{other}) \ \mathsf{p}(\mathsf{VB}|\mathsf{other}) \ \mathsf{p}(\mathsf{is}|\mathsf{VB}) = 0.03 * 0.6 * 0.05 = 0.0009, \\ \mathsf{vtrb}_1(\mathsf{NN}) \ \mathsf{p}(\mathsf{VB}|\mathsf{NN}) \ \mathsf{p}(\mathsf{is}|\mathsf{VB}) = 0.16 * 0.5 * 0.05 = 0.004, \\ \mathsf{vtrb}_1(\mathsf{VB}) \ \mathsf{p}(\mathsf{VB}|\mathsf{VB}) \ \mathsf{p}(\mathsf{is}|\mathsf{VB}) = 0.135 * 0.1 * 0.05 = 0.000675 \\) = 0.004 \\ \mathsf{bptr}_2(\mathsf{VB}) = \mathsf{NN} \end{array}$$

Probability of the most likely path: $0.0192 = \max_t vtrb_2(t)$ Last tag of the most likely path: other = $\arg \max_t vtrb_2(t)$ First tag of the most likely path: NN = $bptr_2(other)$ **Result:**

NN other = arg max_{t_1t_2} $p(t_1, move, t_2, is)$

Besonders klausurrelevant

- Part-of-speech tagging, informal definition
- Part-of-speech tagging, formal definition

$$\operatorname{argmax}_{t_{1,n}} \sum_{i=1}^{n} [\log P(w_i|t_i) + \log P(t_i|t_{i-1})]$$

- Brown part-of-speech tags
- Parameter estimation: Context

$$\hat{P}(t^k|t^j) = rac{C(t^jt^k)}{C(t^j)}$$

• Parameter estimation: Word bias

$$\hat{P}(w^{l}|t^{j}) = \frac{C(w^{l}:t^{j})}{C(t^{j})}$$

- Order of a Markov model
- Viterbi

Schütze: HMMs