

# Einführung in die Computerlinguistik

## Text Classification and Naive Bayes

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2019-01-07

# Outline

- 1 Text classification
- 2 Naive Bayes
- 3 NB theory
- 4 Evaluation of TC

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# A text classification task: Email spam filtering

From: '' <takworldld@hotmail.com>

Subject: real estate is the only way... gem oalvgkay

Anyone can buy real estate with no money down

Stop paying rent TODAY !

There is no need to spend hundreds or even thousands for similar courses

I am 22 years old and I have already purchased 6 properties using the methods outlined in this truly INCREDIBLE ebook.

Change your life NOW !

=====  
Click Below to order:

<http://www.wholesaledaily.com/sales/nmd.htm>  
=====

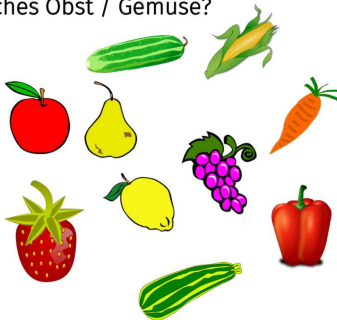
# Mustererkennung (pattern recognition)

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Kamera

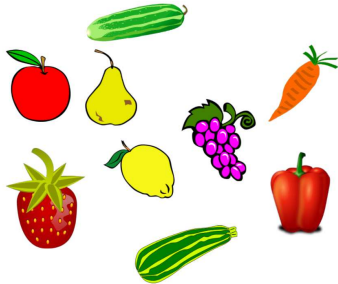
Welches Obst / Gemüse?



Was sind mögliche  
Erkennungsmerkmale?

# Mustererkennung (pattern recognition)

---



Merkmale/Attribute:

- Farbe
- Größe
- Form
- ...

Beispiele:

Attribute/Werte + richtige Klasse



Algorithmus  
(Maschinelles Lernen)



neues  
Objekt



Classifier



Zitrone (80%)  
Birne (20%)

# Formal definition of TC: Training

Given:

- A document space  $\mathbb{X}$

[7]

Using a learning method or **learning algorithm**, we then wish to learn a **classifier**  $\gamma$  that maps documents to classes:

$$\gamma : \mathbb{X} \rightarrow \mathbb{C}$$

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Given:

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- A fixed set of **classes**  $\mathbb{C} = \{c_1, c_2, \dots, c_J\}$ 
  - The classes are human-defined for the needs of an application (e.g., spam vs. nonspam).
- A **training set**  $\mathbb{D}$  of labeled documents. Each labeled document  $\langle d, c \rangle \in \mathbb{X} \times \mathbb{C}$

[7]

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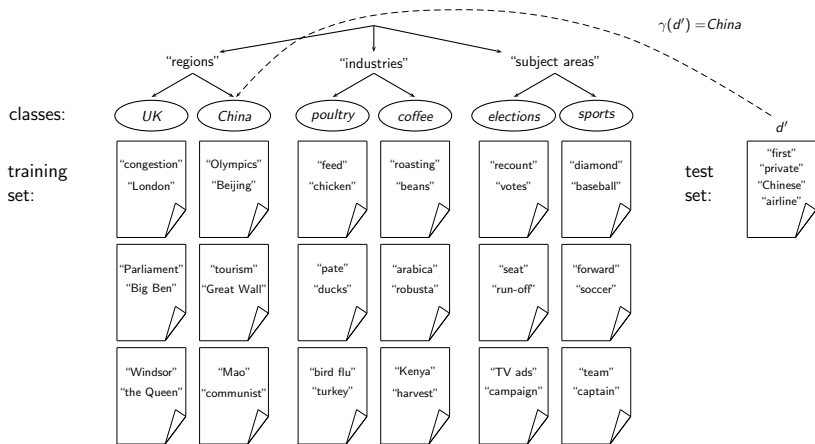
We can view sentences also as documents – so “document” refers to any piece of text we want to classify.

# Formal definition of TC: Application/Testing

Given: a description  $d \in \mathbb{X}$  of a document

Determine:  $\gamma(d) \in \mathbb{C}$ , that is,  
determine the class that is most appropriate for  $d$

# Topic classification



# Applications of text classification

- Language identification  
(classes: English vs French vs . . . )
- The automatic detection of spam pages  
(spam vs nonspam)
- Sentiment analysis:  
Is a movie or product review positive or negative  
(positive vs negative)
- Topic-specific or *vertical* search:  
Restrict search to a “vertical” like “related to health”  
(classes: relevant to vertical vs not)

# Classification methods: 1. Manual

- Manual classification was used by Yahoo in the beginning of the web. Also: ODP, PubMed
- Very accurate if job is done by experts
- Consistent when the problem size and team is small
- Scaling manual classification is difficult and expensive.
- → We need automatic methods for classification.

## Classification methods: 2. Rule-based

- E.g., Google Alerts is rule-based classification.
- There are IDE-type development environments for writing very complex rules efficiently. (e.g., Verity)
- Often: Boolean combinations (as in Google Alerts)
- Accuracy is very high if a rule has been carefully refined over time by a subject expert.
- Building and maintaining rule-based classification systems is cumbersome and expensive.

# A Verity topic (a complex classification rule)

```
comment line      # Beginning of art topic definition
top-level topic   art ACCRUE
                  /author = "fsmith"
topic definition modifiers {
                  /date  = "30-Dec-01"
                  /annotation = "Topic created
                                by fsmith"

subtopic topic    * 0.70 performing-arts ACCRUE
  evidence topic  ** 0.50 WORD
    topic definition modifier /wordtext = ballet
    evidence topic  ** 0.50 STEM
    topic definition modifier /wordtext = dance
    evidence topic  ** 0.50 WORD
    topic definition modifier /wordtext = opera
    evidence topic  ** 0.30 WORD
    topic definition modifier /wordtext = symphony
subtopic          * 0.70 visual-arts ACCRUE
                  ** 0.50 WORD
                  /wordtext = painting
                  ** 0.50 WORD
                  /wordtext = sculpture

subtopic          * 0.70 film ACCRUE
                  ** 0.50 STEM
                  /wordtext = film
subtopic          ** 0.50 motion-picture PHRASE
                  *** 1.00 WORD
                  /wordtext = motion
                  *** 1.00 WORD
                  /wordtext = picture
```

# Classification methods: 3. Statistical/Probabilistic

- This was our definition of the classification problem:  
Text classification as a learning problem
- (i) Supervised learning of a the classification function  $\gamma$  and  
(ii) application of  $\gamma$  to classifying new documents
- We will look at one method for doing this:  
Naive Bayes
- No free lunch: requires hand-classified training data
- But this manual classification can be done by non-experts.

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# The Naive Bayes classifier

- The Naive Bayes classifier is a probabilistic classifier.
- We compute the probability of a document  $d$  being in a class  $c$  as follows:

$$P(c|d) \propto P(c) \prod_{1 \leq k \leq n_d} P(t_k|c)$$

- $n_d$  is the length of the document. (number of tokens)
- $P(t_k|c)$  is the **conditional probability** of term  $t_k$  occurring in a document of class  $c$
- $P(t_k|c)$  is a measure of **how much evidence**  $t_k$  contributes that  $c$  is the correct class.
- $P(c)$  is the **prior probability** of  $c$ .
- If a document's terms do not provide clear evidence for one class vs. another, we choose the  $c$  with highest  $P(c)$ .

# Maximum a posteriori class

- Goal in Naive Bayes classification:  
Find the “best” class
- The best class is the most likely or **maximum a posteriori (MAP) class**  $c_{\text{map}}$ :

$$c_{\text{map}} = \operatorname{argmax}_{c \in \mathbb{C}} \hat{P}(c|d) = \operatorname{argmax}_{c \in \mathbb{C}} \hat{P}(c) \prod_{1 \leq k \leq n_d} \hat{P}(t_k|c)$$

# Taking the log

- Multiplying lots of small probabilities can result in floating point underflow.
- Since  $\log(xy) = \log(x) + \log(y)$ , we can sum log probabilities instead of multiplying probabilities.
- Since log is a monotonic function, the class with the highest score does not change.
- So what we usually compute in practice is:

$$c_{\text{map}} = \operatorname{argmax}_{c \in \mathbb{C}} [\log \hat{P}(c) + \sum_{1 \leq k \leq n_d} \log \hat{P}(t_k | c)]$$

# Naive Bayes classifier

- Classification rule:

$$c_{\text{map}} = \operatorname{argmax}_{c \in \mathbb{C}} [\log \hat{P}(c) + \sum_{1 \leq k \leq n_d} \log \hat{P}(t_k | c)]$$

- Simple interpretation:

- Each conditional parameter  $\log \hat{P}(t_k | c)$  is a weight that indicates how good an indicator  $t_k$  is for  $c$ .
- The prior  $\log \hat{P}(c)$  is a weight that indicates the relative frequency of  $c$ .
- The sum of log prior and term weights is then a measure of how much evidence there is for the document being in the class.
- We select the class with the most evidence.

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  - We select the class with the most evidence.

# Parameter estimation take 1: Maximum likelihood

- Estimate parameters  $\hat{P}(c)$  and  $\hat{P}(t_k|c)$  from train data: How?
- Prior:

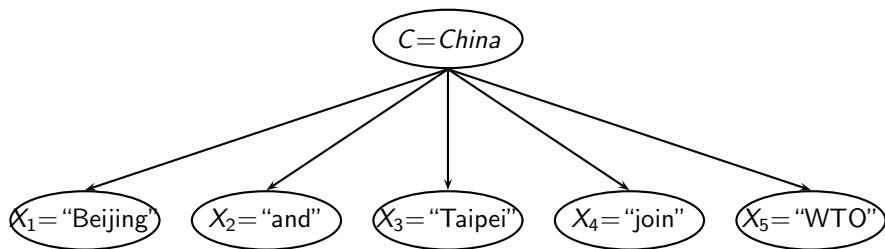
$$\hat{P}(c) = \frac{N_c}{N}$$

- $N_c$ : number of docs in class  $c$ ;  $N$ : total number of docs
- Conditional probabilities:

$$\hat{P}(t|c) = \frac{T_{ct}}{\sum_{t' \in V} T_{ct'}}$$

- $T_{ct}$  is the number of tokens of  $t$  in training documents from class  $c$  (includes multiple occurrences)

# The problem with maximum likelihood estimates: Zeros

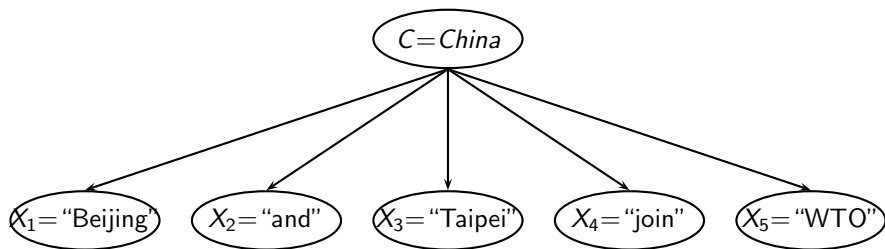


$$P(\text{China}|d) \propto P(\text{China}) \cdot P(\text{"Beijing"}|\text{China}) \cdot P(\text{"and"}|\text{China}) \\ \cdot P(\text{"Taipei"}|\text{China}) \cdot P(\text{"join"}|\text{China}) \cdot P(\text{"WTO"}|\text{China})$$

- If "WTO" never occurs in class China in the train set:

$$\hat{P}(\text{"WTO"}|\text{China}) = \frac{T_{\text{China}, \text{"WTO"}}}{\sum_{t' \in V} T_{\text{China}, t'}} = \frac{0}{\sum_{t' \in V} T_{\text{China}, t'}} = 0$$

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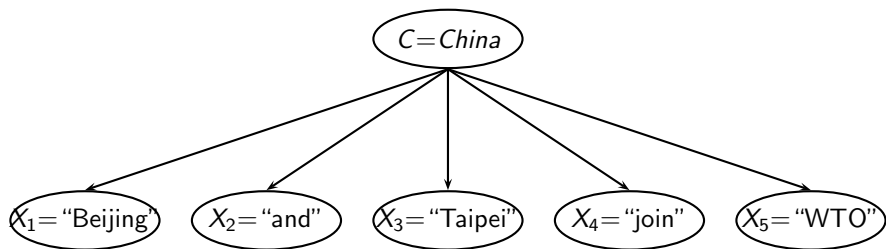


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- If "WTO" never occurs in class China in the train set:

$$\textcolor{red}{\hat{P}(\text{"WTO"}|\text{China})} = \frac{T_{\text{China}, \text{"WTO"}}}{\sum_{t' \in V} T_{\text{China}, t'}} = \frac{0}{\sum_{t' \in V} T_{\text{China}, t'}} = 0$$

# The problem with maximum likelihood estimates: Zeros (cont)

- If there are no occurrences of “WTO” in documents in class China, we get a zero estimate:

$$\hat{P}(\text{“WTO”} | China) = \frac{T_{China, \text{“WTO”}}}{\sum_{t' \in V} T_{China, t'}} = 0$$

- $\rightarrow$  We will get  $P(China|d) = 0$  for any document that contains WTO!

# To avoid zeros: Add-one smoothing

- Before:

$$\hat{P}(t|c) = \frac{T_{ct}}{\sum_{t' \in V} T_{ct'}}$$

- Now: Add one to each count to avoid zeros:

$$\hat{P}(t|c) = \frac{T_{ct} + 1}{\sum_{t' \in V} (T_{ct'} + 1)} = \frac{T_{ct} + 1}{(\sum_{t' \in V} T_{ct'}) + B}$$

- $B$  is the number of bins – in this case the number of different words or the size of the vocabulary  $|V| = M$

# Naive Bayes: Summary

- Estimate parameters from the training corpus using add-one smoothing
- For a new document, for each class, compute sum of (i) log of prior and (ii) logs of conditional probabilities of the terms
- Assign the document to the class with the largest score

# Naive Bayes: Training

TRAINMULTINOMIALNB( $\mathbb{C}, \mathbb{D}$ )

```
1   $V \leftarrow \text{EXTRACTVOCABULARY}(\mathbb{D})$ 
2   $N \leftarrow \text{COUNTDOCS}(\mathbb{D})$ 
3  for each  $c \in \mathbb{C}$ 
4  do  $N_c \leftarrow \text{COUNTDOCSINCLASS}(\mathbb{D}, c)$ 
5      $\text{prior}[c] \leftarrow N_c / N$ 
6      $\text{text}_c \leftarrow \text{CONCATENATETEXTOFALLDOCSINCLASS}(\mathbb{D}, c)$ 
7     for each  $t \in V$ 
8     do  $T_{ct} \leftarrow \text{COUNTTOKENSOFTERM}(\text{text}_c, t)$ 
9     for each  $t \in V$ 
10    do  $\text{condprob}[t][c] \leftarrow \frac{T_{ct}+1}{\sum_{t'} (T_{ct'}+1)}$ 
11 return  $V, \text{prior}, \text{condprob}$ 
```

# Naive Bayes: Testing

APPLYMULTINOMIALNB( $\mathbb{C}$ ,  $V$ ,  $prior$ ,  $condprob$ ,  $d$ )

1  $W \leftarrow \text{EXTRACTTOKENSFROMDOC}(V, d)$

2 **for each**  $c \in \mathbb{C}$

3 **do**  $score[c] \leftarrow \log prior[c]$

4     **for each**  $t \in W$

5         **do**  $score[c] += \log condprob[t][c]$

6 **return**  $\text{argmax}_{c \in \mathbb{C}} score[c]$

## Exercise: Estimate parameters, classify test set

	docID	words in document	in $c = \textit{China}$ ?
training set	1	Chinese Beijing Chinese	yes
	2	Chinese Chinese Shanghai	yes
	3	Chinese Macao	yes
	4	Tokyo Japan Chinese	no
test set	5	Chinese Chinese Chinese Tokyo Japan	?

$$\hat{P}(c) = \frac{N_c}{N}$$

$$\hat{P}(t|c) = \frac{T_{ct} + 1}{\sum_{t' \in V} (T_{ct'} + 1)} = \frac{T_{ct} + 1}{(\sum_{t' \in V} T_{ct'}) + B}$$

( $B$  is the number of bins – in this case the number of different words or the size of the vocabulary  $|V| = M$ )

$$c_{\text{map}} = \operatorname{argmax}_{c \in C} [\hat{P}(c) \cdot \prod_{1 \leq k \leq n_d} \hat{P}(t_k|c)]$$



## Example: Parameter estimates

Priors:  $\hat{P}(c) = 3/4$  and  $\hat{P}(\bar{c}) = 1/4$

Conditional probabilities:

$$\hat{P}(\text{"Chinese"} | c) = (5 + 1)/(8 + 6) = 6/14 = 3/7$$

$$\hat{P}(\text{"Tokyo"} | c) = \hat{P}(\text{"Japan"} | c) = (0 + 1)/(8 + 6) = 1/14$$

$$\hat{P}(\text{"Chinese"} | \bar{c}) = (1 + 1)/(3 + 6) = 2/9$$

$$\hat{P}(\text{"Tokyo"} | \bar{c}) = \hat{P}(\text{"Japan"} | \bar{c}) = (1 + 1)/(3 + 6) = 2/9$$

The denominators are  $(8 + 6)$  and  $(3 + 6)$  because the lengths of  $text_c$  and  $text_{\bar{c}}$  are 8 and 3, respectively, and because the constant  $B$  is 6 as the vocabulary consists of six terms.

## Example: Classification

$$\hat{P}(c|d_5) \propto 3/4 \cdot (3/7)^3 \cdot 1/14 \cdot 1/14 \approx 0.0003$$

$$\hat{P}(\bar{c}|d_5) \propto 1/4 \cdot (2/9)^3 \cdot 2/9 \cdot 2/9 \approx 0.0001$$

Thus, the classifier assigns the test document to  $c = \textit{China}$ . The reason for this classification decision is that the three occurrences of the positive indicator “Chinese” in  $d_5$  outweigh the occurrences of the two negative indicators “Japan” and “Tokyo”.

## UNK

An UNK is a word that occurs in the test set, but did not occur in the training set.

- Option 1: Simply ignore UNKs
- Option 2: Add UNK to the training vocabulary
  - All counts  $T_{c\text{UNK}}$  are zero (since UNK does not occur in training set).
  - All words in the test set that did not occur in the training set are replaced by “UNK”.

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# Naive Bayes: Analysis

- Now we want to gain a better understanding of the properties of Naive Bayes.
- We will formally derive the classification rule ...
- ...and make our assumptions explicit.

# Derivation of Naive Bayes rule

We want to find the class that is most likely given the document:

$$c_{\text{map}} = \operatorname{argmax}_{c \in \mathbb{C}} P(c|d)$$

Apply Bayes rule  $P(A|B) = \frac{P(B|A)P(A)}{P(B)}$ :

$$c_{\text{map}} = \operatorname{argmax}_{c \in \mathbb{C}} \frac{P(d|c)P(c)}{P(d)}$$

Drop denominator since  $P(d)$  is the same for all classes:

$$c_{\text{map}} = \operatorname{argmax}_{c \in \mathbb{C}} P(d|c)P(c)$$

# Too many parameters / sparseness

$$\begin{aligned}c_{\text{map}} &= \operatorname{argmax}_{c \in \mathbb{C}} P(d|c)P(c) \\ &= \operatorname{argmax}_{c \in \mathbb{C}} P(\langle t_1, \dots, t_k, \dots, t_{n_d} \rangle | c)P(c)\end{aligned}$$

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- There are too many parameters  $P(\langle t_1, \dots, t_k, \dots, t_{n_d} \rangle | c)$ , one for each unique combination of a class and a sequence of words.

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- We would need a very, very large number of training examples to estimate that many parameters.

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- There are too many parameters  $P(\langle t_1, \dots, t_k, \dots, t_{n_d} \rangle | c)$ , one for each unique combination of a class and a sequence of words.
- We would need a very, very large number of training examples to estimate that many parameters.
- This is the problem of **data sparseness**.

# Bag of words model

To reduce the number of parameters to a manageable size, we make the **Naive Bayes conditional independence assumption**:

$$P(d|c) = P(\langle t_1, \dots, t_{n_d} \rangle | c) = \prod_{1 \leq k \leq n_d} P(X_k = t_k | c)$$

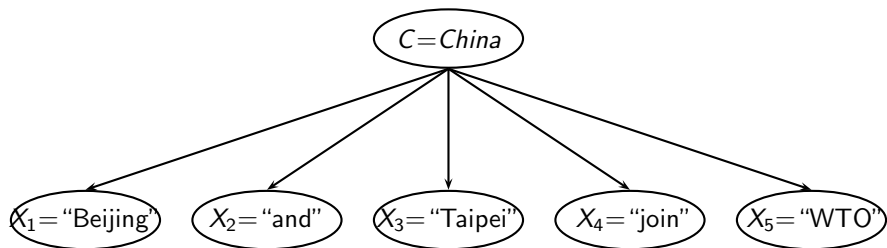
We assume that the probability of observing the conjunction of attributes is equal to the product of the individual probabilities  $P(X_k = t_k | c)$ .

Recall from earlier the estimates for these conditional probabilities:

$$\hat{P}(t|c) = \frac{T_{ct} + 1}{(\sum_{t' \in V} T_{ct'}) + B}$$

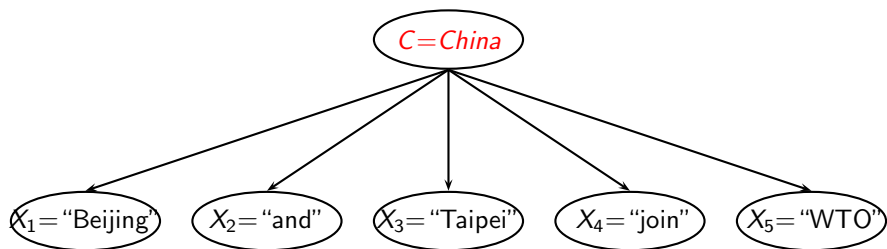
**Bag of words model**

# Generative model



$$P(c|d) \propto P(c) \prod_{1 \leq k \leq n_d} P(t_k|c)$$

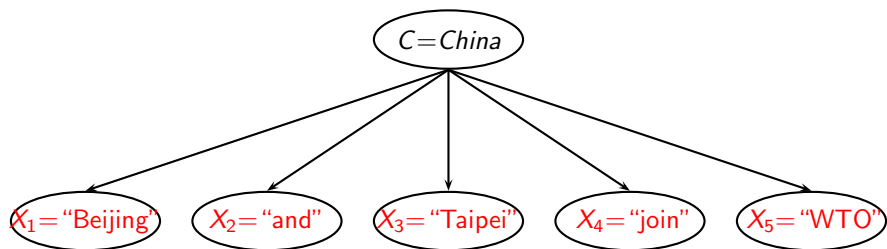
# Generative model



$$P(c|d) \propto P(c) \prod_{1 \leq k \leq n_d} P(t_k|c)$$

- Generate a class with probability  $P(c)$

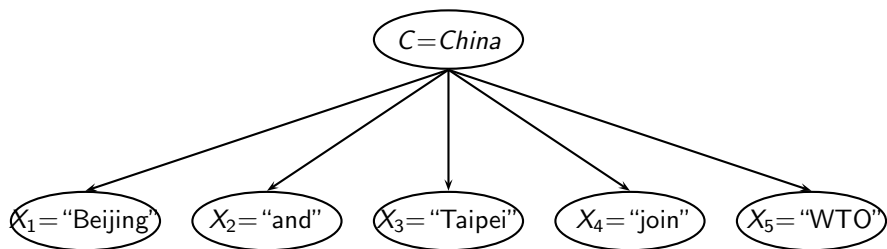
# Generative model



$$P(c|d) \propto P(c) \prod_{1 \leq k \leq n_d} P(t_k|c)$$

- Generate a class with probability  $P(c)$
- Generate each of the words (in their respective positions), conditional on the class, but independent of each other, with probability  $P(t_k|c)$

# Generative model



$$P(c|d) \propto P(c) \prod_{1 \leq k \leq n_d} P(t_k|c)$$

- Generate a class with probability  $P(c)$
- Generate each of the words (in their respective positions), conditional on the class, but independent of each other, with probability  $P(t_k|c)$
- To classify docs, we “reengineer” this process and find the class that is most likely to have generated the doc.

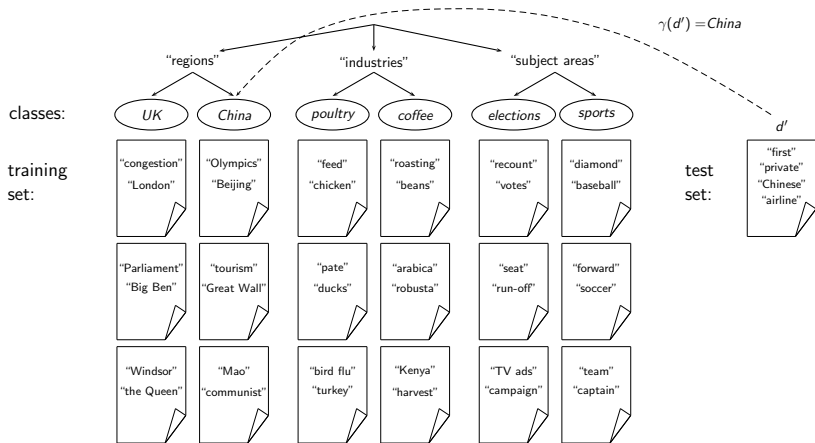
# Naive Bayes is not so naive

- Naive Bayes has won some bakeoffs (e.g., KDD-CUP 97)
- More robust to nonrelevant features than some more complex learning methods
- More robust to concept drift (changing of definition of class over time) than some more complex learning methods
- Better than methods like decision trees when we have **many equally important features**
- A good dependable baseline for text classification (but not the best)
- Optimal if independence assumptions hold (never true for text, but true for some domains)
- Very fast
- Low storage requirements

# Outline

- 1 Text classification
- 2 Naive Bayes
- 3 NB theory
- 4 Evaluation of TC**

# Evaluation on Reuters



## Example: The Reuters collection

symbol	statistic	value
$N$	documents	800,000
$L$	avg. # word tokens per document	200
$M$	word types	400,000

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$N$	documents	800,000
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type of class	number	examples
region	366	UK, China
industry	870	poultry, coffee
subject area	126	elections, sports



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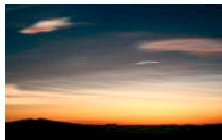
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## Extreme conditions create rare Antarctic clouds

Tue Aug 1, 2006 3:20am ET

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SYDNEY (Reuters) - Rare, mother-of-pearl colored clouds caused by extreme weather conditions above Antarctica are a possible indication of global warming, Australian scientists said on Tuesday.

Known as nacreous clouds, the spectacular formations showing delicate wisps of colors were photographed in the sky over an Australian

# Evaluating classification

- Evaluation must be done on test data that are independent of the training data, i.e., training and test sets are disjoint.
- It's easy to get good performance on a test set that was available to the learner during training (e.g., just memorize the test set).
- Measures: Precision, recall,  $F_1$ , classification accuracy

# Precision $P$ and recall $R$

	in the class	not in the class
predicted to be in the class	true positives (TP)	false positives (FP)
predicted to not be in the class	false negatives (FN)	true negatives (TN)

TP, FP, FN, TN are counts of documents. The sum of these four counts is the total number of documents.

$$\text{precision: } P = TP / (TP + FP)$$

$$\text{recall: } R = TP / (TP + FN)$$

# Precision/recall tradeoff

- You can **easily increase recall** by returning more results.
- Recall is a non-decreasing function of the number of results returned.
- A system that returns everything has 100% recall!
- The converse is also true (usually): **It's easy to get high precision** for very low recall.
- In most application scenarios, we need both good precision and good recall.
- So we need to find a good **precision-recall** tradeoff.

# A combined measure: $F_1$

- $F_1$  allows us to trade off precision against recall.



$$F_1 = \frac{1}{\frac{1}{2} \frac{1}{P} + \frac{1}{2} \frac{1}{R}} = \frac{2PR}{P + R}$$

- This is the **harmonic mean** of  $P$  and  $R$ :  $\frac{1}{F} = \frac{1}{2}(\frac{1}{P} + \frac{1}{R})$
- The harmonic mean is a kind of “soft” minimum.

$$\text{accuracy} = \frac{TP + TN}{TP + TN + FP + FN}$$

# $F_1$ scores for Naive Bayes vs. other methods

(a)	NB	Rocchio	kNN	SVM
micro-avg-L (90 classes)	80	85	86	89
macro-avg (90 classes)	47	59	60	60

(b)	NB	Rocchio	kNN	trees	SVM
earn	96	93	97	98	98
acq	88	65	92	90	94
money-fx	57	47	78	66	75
grain	79	68	82	85	95
crude	80	70	86	85	89
trade	64	65	77	73	76
interest	65	63	74	67	78
ship	85	49	79	74	86
wheat	70	69	77	93	92
corn	65	48	78	92	90
micro-avg (top 10)	82	65	82	88	92
micro-avg-D (118 classes)	75	62	n/a	n/a	87

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Naive Bayes does pretty well, but some methods beat it consistently (e.g., SVM).

# Confusion matrix for Reuters-21578

	assigned class:	<i>money-fx</i>	<i>trade</i>	<i>interest</i>	<i>wheat</i>	<i>corn</i>	<i>grain</i>
true class:							
<i>money-fx</i>		95	0	10	0	0	0
<i>trade</i>		1	1	90	0	1	0
<i>interest</i>		13	0	0	0	0	0
<i>wheat</i>		0	0	1	34	3	7
<i>corn</i>		1	0	2	13	26	5
<i>grain</i>		0	0	2	14	5	10

Example: 14 documents from *grain* were incorrectly assigned to *wheat*.

# Exercise

Compute precision, recall and  $F_1$ :

	in class	not in class
predicted to be in class	TP: 18	FP: 2
predicted not to be in class	FN: 82	TN: 1,000,000,000

$$\text{precision: } P = TP / (TP + FP)$$

$$\text{recall: } R = TP / (TP + FN)$$

$$F_1 = \frac{2PR}{P + R}$$

- What is text classification?  
(or: What is sentence classification?)
- Naive Bayes classification rule
- Estimation of Naive Bayes priors and conditionals
- Theory: Bag of words model
  - Maximum likelihood
  - Add-one = Laplace
- Precision, recall,  $F_1$
- Precision-recall tradeoff
- Confusion matrix